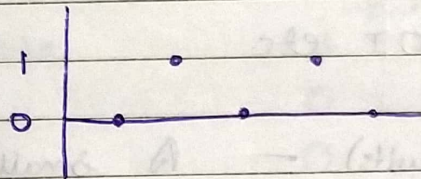
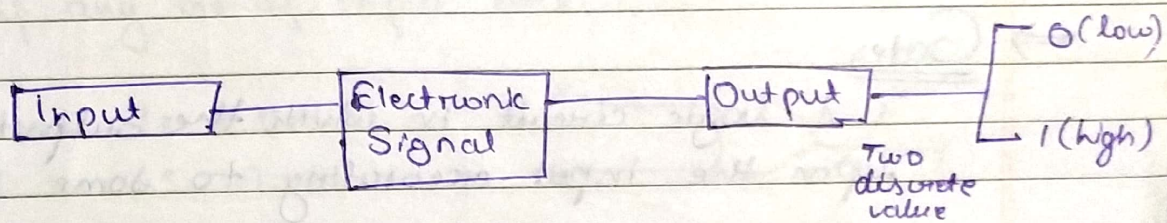


⇒ Digital Electronic - is the branch of electronic which deals with a digital signals to perform various task to meet various requirement.

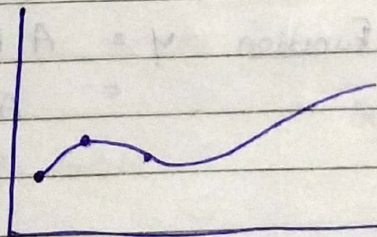
The input signal applied to this circuit is of digital form which is represented in 0 & 1 (binary lang. format) for example - electronic calculator.



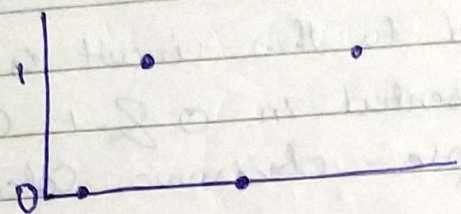
⇒ what is signal?

A signal is a function, that represent the variation of a physical quantity with respect to any parameter.

⇒ Analog Signal - A continuous signal that can have any values in a given range it is also known as Continuous signals.



⇒ Digital Signal - Signal with only two discrete values these are usually represented by low and high for 0 & 1.



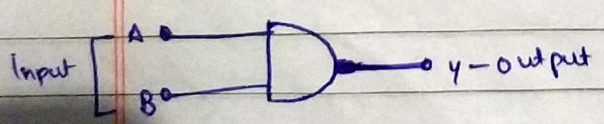
⇒ Gates  
A logic circuit in which the output depends upon the input according to some logic rules.

like - AND, OR, NOT etc

⇒ ICs (Integrated Circuits) - A small semiconductor chip containing several electronic circuit.

⇒ Truth table - A table that gives output for all possible combination of input to a logic circuit.

⇒ AND Operation - A logic circuit whose output is 1 if and only if all the inputs are 1.

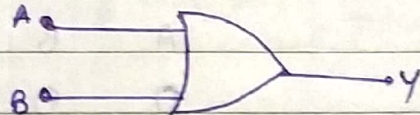


Function  $y = A \text{ AND } B$   
 $= A \cdot B$

Truth table	Inputs		output
	A	B	Y
	0	0	0
	0	1	0
	1	0	0
	1	1	1

⇒ OR operation - A logic circuit whose output is 1 if any one of input are 1.

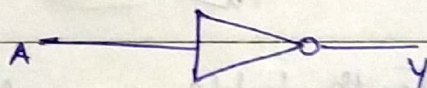
function  $Y = A \text{ OR } B$   
 $= A + B$



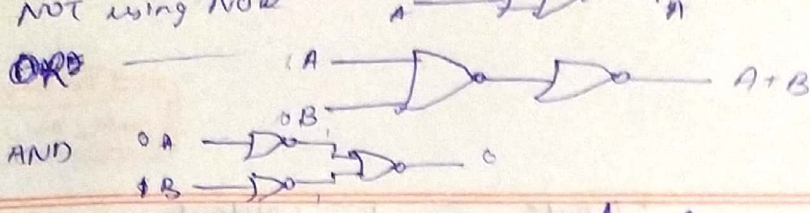
Truth table	Inputs		output
	A	B	Y
	0	0	0
	0	1	1
	1	0	1
	1	1	1

⇒ NOT operation - A logic circuit in which we give one input and get one output and its also known as inverter. It gives output inverse of input.

function  $Y = \text{NOT } A$   
 $= \bar{A}$

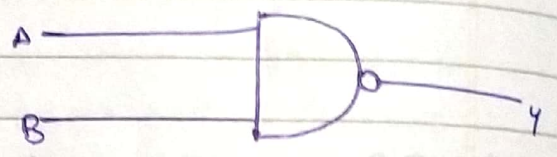


Truth table	Input	output
	A	Y
	0	1
	1	0



⇒ NAND operation - A logic gate whose output is zero if any and only if all its input is logic one.

function  $Y = A \text{ NAND } B$   
 $= A \text{ NOT AND } B$   
 $= \overline{AB}$

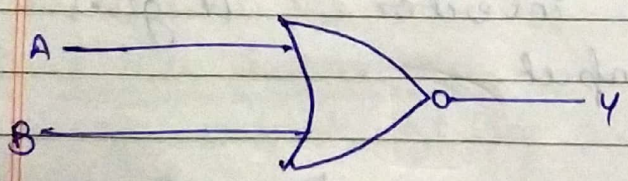


Truth table

A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

⇒ NOR operation - A logic gate whose output is zero if any of input is one.

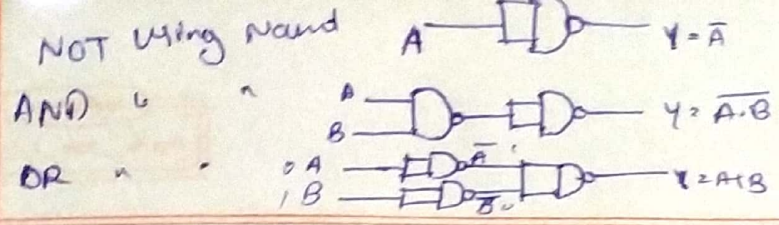
A logic gate whose output is one if and only if all its input are logic is zero.



function  $Y = A \text{ NOR } B$   
 $Y = A \text{ NOT OR } B$   
 $= \overline{A+B}$

Truth table

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0



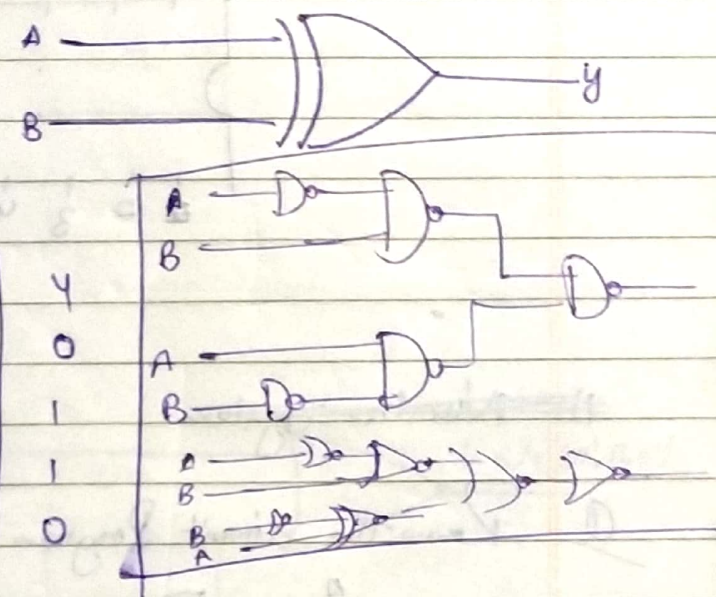
⇒ Exclusive OR - Gate / 'XOR' Gate

A two input gate whose output is logic zero if both the input are equal and one when the inputs are unequal.

function  $Y = A \oplus B$   
 $A \oplus B$   
 $\bar{A}B + A\bar{B}$

Truth table

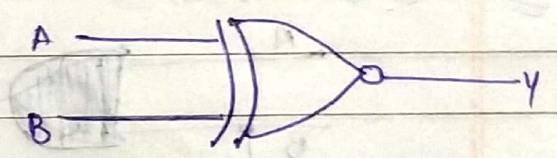
A	B	Y
0	0	0
1	0	1
0	1	1
1	1	0



⇒ Exclusive NOR Gate - / X-NOR

A two input gate whose output is logic one when both the input are same.

function  $Y = A \odot B$   
 $\bar{A \oplus B}$   
 $A \odot B$

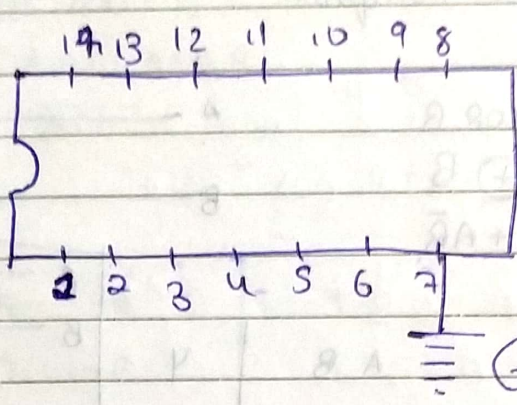


Truth table

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

# \* Integrated Circuit (IC)

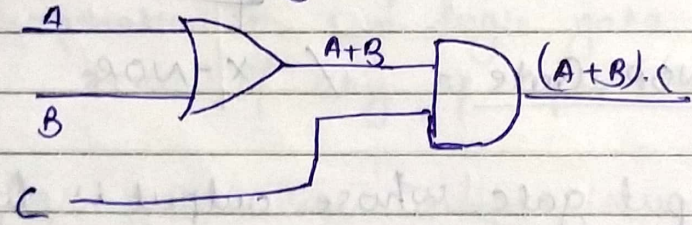
IC or Integrated circuit is a small semiconductor chip containing several electronic circuits.



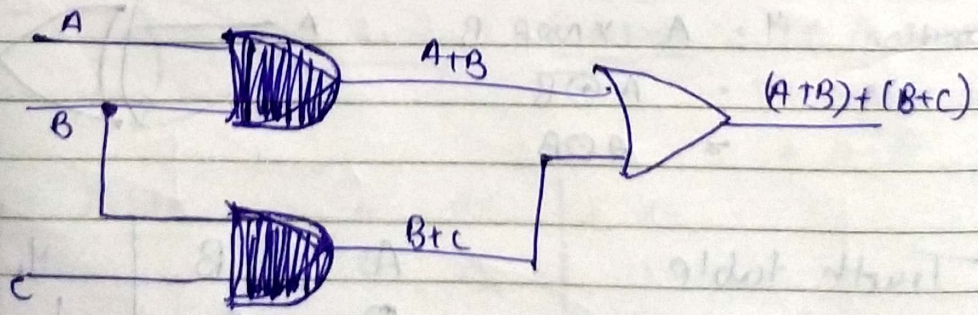
NOT	7404
AND	7408
OR	7432
NAND	7400
NOR	7402
Ex OR	7486

## ~~# Number System~~

Q Draw the circuit Program of  $(A+B).C$



Q  $(A \cdot B) + (B \cdot C)$



# Boolean Algebraic Theorem

$$A + 0 = A$$

$$A \cdot 1 = A$$

$$A + 1 = 1$$

$$A \cdot 0 = 0$$

$$A + A = A$$

$$A \cdot A = A$$

$$A + \bar{A} = 1$$

$$A \cdot \bar{A} = 0$$

$$A \cdot (B + C) = AB + AC$$

$$A + BC = (A + B)(A + C)$$

$$A + AB = A$$

$$A(A + B) = A$$

$$A + \bar{A}B = (A + B)$$

$$A(\bar{A} + B) = AB$$

$$AB + \bar{A}B = B$$

$$(A + B)(A + \bar{B}) = A$$

$$AB + \bar{A}C = (A+C)(\bar{A}+B)$$

$$(A+B)(\bar{A}+C) = A\bar{A} + AC + B\bar{A} + BC$$

$$AB + \bar{A}C + BC = AB + \bar{A}C$$

$$(A+B)(\bar{A}+C)(B+C) = (A+B)(\bar{A}+C)$$

$$A \cdot B \cdot C = \bar{A} + B + C + \dots$$

$$A+B+C = \bar{A} \cdot \bar{B} \cdot \bar{C} + \dots$$

## Number Systems

### ⇒ Binary to Decimal ( $\times 2^n$ )

Ex (1111)<sub>2</sub> → ( )<sub>10</sub>

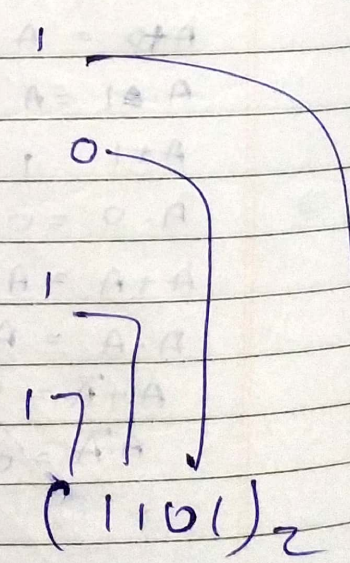
$$1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$8 + 4 + 2 + 1 = (15)_{10} \quad \text{Yes}$$

### ⇒ Decimal to Binary

Ex (13)<sub>10</sub> → ( )<sub>2</sub>

13	6
6	3
3	1
1	0



⇒  $(0.65625)_{10} \rightarrow ( )_2$

$0.65625$ $\times 2$	$1.31250$ $\times 2$	$0.62500$ $\times 2$	$1.25000$ $\times 2$	$0.50000$ $\times 2$	$1.00000$ $\times 2$
$1.31250$	$0.62500$	$1.25000$	$0.50000$	$1.00000$	$1.00000$
1	0	1	0	1	1

$(0.65625)_{10} \rightarrow (10101)_2$

⇒ Signed Binary number  $\rightarrow$  Decimal.

$(101100)_2 \rightarrow (-12)_{10}$

1 = -  
0 = +

$(010000)_2 \rightarrow (+8)_{10}$

⇒ One's Complement

$010011001 \rightarrow 1011000110$

⇒ Two Complement

i)  $01001110 \rightarrow$  Complement + 1  $\text{ⓐ}$

$01001110 \rightarrow$

$10110001$   
 $+ 1$

$\hline 10110010$   
 $\hline$

## → Binary Addition

		Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$\begin{array}{r}
 \phantom{+} 1011 \\
 + 1100 \\
 \hline
 10111 \\
 \text{Carry}
 \end{array}$$

$$\begin{array}{r}
 \phantom{+} 0101 \\
 + 1111 \\
 \hline
 10100 \\
 \text{Carry}
 \end{array}$$

## → Binary Subtraction

		Difference	Borrow
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$\begin{array}{r}
 1011 \\
 - 0111 \\
 \hline
 0100
 \end{array}$$

⇒ Binary Multiplication

$$\begin{array}{r}
 1001 \\
 \times 1001 \\
 \hline
 1001 \\
 0000x \\
 1001xx \\
 1001xxx \\
 \hline
 1110101
 \end{array}$$

⇒ Binary Division

$$\begin{array}{r}
 1101 \\
 100 \overline{) 1110101} \\
 \underline{1001} \phantom{00} \\
 01011 \\
 \underline{1001} \\
 10001 \\
 \underline{1001} \\
 \hline
 b
 \end{array}$$

⇒ Complement Arithmetic (Add/Sub in 2's comp rep)

$$\begin{array}{r}
 48 - 23 \\
 \hline
 2's \text{ complement rep of } +48 = 10
 \end{array}$$

Octal number system.

The no system with base (or radix) 8 is known as octal number system. In this system symbols 0, 1, 2, 3, 4, 5, 6, 7 are used to represent no.

⇒ Octal → decimal

$(6327.4051)_8 \rightarrow ( )_{10}$

$$6 \times 8^3 + 3 \times 8^2 + 2 \times 8^1 + 7 \times 8^0 + 4 \times 8^{-1} + 0 \times 8^{-2} + 5 \times 8^{-3} + 1 \times 8^{-4}$$

$$3072 + 192 + 16 + 7 + \frac{4}{2} + 0 + \frac{5}{512} + \frac{1}{4096}$$

$(3287.51001)_{10}$

⇒ Decimal to Octal

$(247)_{10} \rightarrow ( )_8$

$\frac{247}{8}$	30	7
$\frac{30}{8}$	3	6
$\frac{3}{8}$	0	3

$(367)_8$

$(0.6875)_{10} \rightarrow ( )_8$

$0.6875$	$0.5$
$\times 8$	$\times 8$
<hr/>	<hr/>
5.5	4.0

$(0.54)_8$

## Octal to Binary Conversion

Octal number can be converted into equivalent binary number by replace each octal digit by its 3 bit equivalent binary. In octal number we can take 0 to 7 decimal

$$(736)_8 \longrightarrow ( )_2$$

8 4 2 1  
case

$$(0111 \ 011 \ 110)_2$$

$$( )_2 \rightarrow ( )_8$$

$$(\underline{100} \ \underline{111} \ \underline{0})_2 \rightarrow ( )_8$$

$$(116)_8$$

$$(0.\underline{101} \ \underline{001} \ \underline{110})_2 \rightarrow ( )_8$$

$$\underline{101} \ \underline{001} \ \underline{100}$$

$$(0.514)_8$$

$$\underline{011001110001} \cdot \underline{000101111001}$$

$$(3161.0871)_8$$

### Octal Arithmetic

23	=	0 1 6 0 1 1
+ 67	=	+ 1 1 0 1 1 1
<u>(112)<sub>8</sub></u>		1 0 0 1 0 1 0
		<u>carry</u>

Hexadecimal NS

⇒ ( )<sub>16</sub> → ( )<sub>10</sub>

10 = A	12 = C	14 = E
11 = B	13 = D	15 = F

(3A.2F)<sub>16</sub> → ( )<sub>10</sub>

$$3 \times 16^1 + 10 \times 16^0 + 2 \times 16^{-1} + 15 \times 16^{-2}$$

$$= (58.1875)_{10}$$

⇒ ( )<sub>10</sub> → ( )<sub>16</sub>  
(98.5)<sub>10</sub> → ( )<sub>16</sub>

98	8	.5	(F)	
5	0	5	(8)	.5
16				x 16
				8.0

(5F.8)<sub>16</sub>

( )<sub>16</sub> → ( )<sub>2</sub>      4 bit

(2F9A)<sub>16</sub> → (0010 1111 1001 1010)<sub>2</sub>

( )<sub>2</sub> → ( )<sub>16</sub>

(0010 1111 1001 1010)<sub>2</sub>  
2 F 9 A F  
(2F9A)<sub>16</sub>

16  
32  
48  
64  
80  
96

$( )_{16} \rightarrow ( )_8$

$(A72E)_{16} \rightarrow (1010 \ 0111 \ 0010 \ 1110)_2$

$(\underline{001010011100101110})_2 \rightarrow ( )_8$

$(123456)_8$

2's Complement Arithmetic

~~7~~     ~~0111~~  
~~-5~~     ~~+1101~~  
            ~~1100~~

3

7 → 0111

-5     1101 ← find 2's complement

~~010~~  
 +1  
 1101

~~8~~  
~~-7~~

0101  
 +111

000  
 +1  
 001

7  
 -5

0111  
 +1101  
 10010  
 Discard ~~1~~  
 0011

0101  
 +1001  
 1110

The final carry is 0

∴ answer is negative and is in 2's comp form

2's comp of 110 = 0010

∴  $(-2)_{10}$

# Codes

- **Weighted Codes**  
eg Binary code  
8421 code  
2421 etc
- **Non weighted**  
eg XS-3  
gray code
- **Reflective (self complementary)**  
eg 2421 code  
XS-3
- **Sequentially code**  
eg 8421  
XS-3
- **Alphanumeric code**  
eg ASCII
- **Error Detecting & Correcting codes**  
eg Hamming code

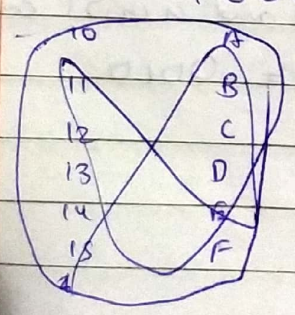
ASCII — American standard code for information interchange

→ BCD (Binary coded Decimal) Code — 8421

Decimal	BCD
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001

Decimal → BCD  
(17)<sub>10</sub> → (0001 0111) BCD

Compare Binary & BCD  
(10)<sub>10</sub> → Binary → BCD  
1010 → (0001 0000)



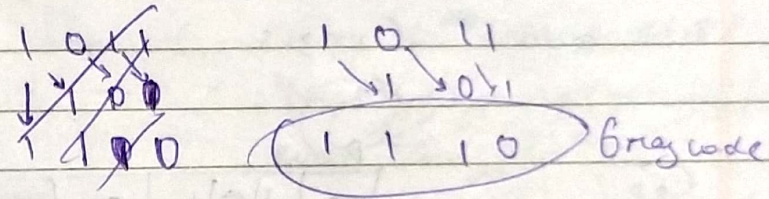
~~XXXXXXXXXX~~ Shift 3 Add 2421 Code

Exer 3

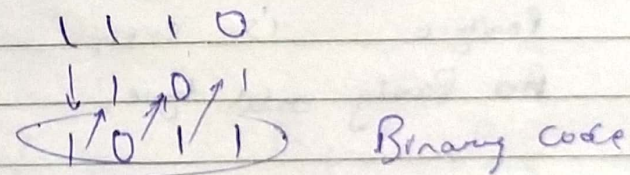
	5	→	0101	+3	→	0101 0011 <hr/> 1000	
			X5-3				24
0	0001		0000				0010 0100
1	0001		0100				0011 0011
2	0010		0101				0101 0111
3	0011		0110				5 7 X5 code for 24
4	0100		0111				
5	0101		1000				
6	0110		1001				
7	0111		1010				
8	1000		1011				
9	1001		1100				

Gray code (Cyclic code)

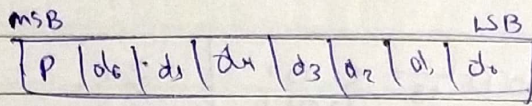
Binary → GC



GC → Binary



→ Parity The simplest technique for detecting errors is to add an extra bit known as parity bit to each word being transmitted

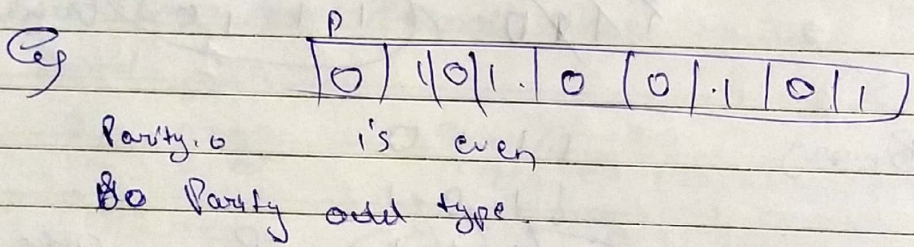


The parity of 8 bit transmitted word can be either even or odd parity

→ Even parity means the number of 1's in the given word including the parity bit should be even (2, 4, 6, 8)

odd - (1, 3, 5, 7)

- i) Even  $\rightarrow$  (2, 4, 6, 8)  $\rightarrow$  0
- (1, 3, 5, 7)  $\rightarrow$  1
- ii) odd (1, 3, 5, 7)  $\rightarrow$  0
- (2, 4, 6, 8)  $\rightarrow$  1

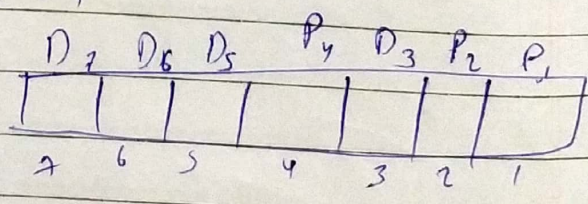
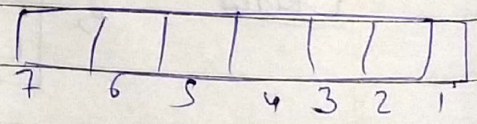


Hamming code

- Data bits - 4
- Parity bits - 3

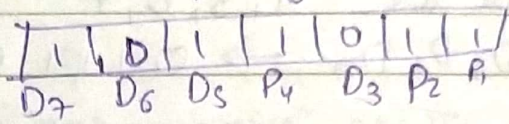
Position for parity bit

- $2^0 = 1$
- $2^1 = 2$
- $2^2 = 4$



- ⇒ Selection  $P_1$  → consider bits 1, 3, 5, 7, 9, 11, 13, 15
- $P_2$  → \_\_\_\_\_ 2, 3, 6, 7, 10, 11, 14, 15
- $P_3$  → \_\_\_\_\_ 4, 5, 6, 7, 12, 13, 14, 15
- $P_4$  → \_\_\_\_\_ 8, 9, 10, 11, 12, 13, 14, 15

1011011 with even parity check code correct or not.



$P_1$   $D_3$   $D_5$   $D_7$   
1 0 1 1

There is error exist  
 $P_1 = 1$

$P_2$   $D_3$   $D_6$   $D_7$   
1 0 0 1

No error  
 $P_2 = 0$

$P_4$   $D_5$   $D_6$   $D_7$   
1 1 0 1

There is error exist  $P_4 = 1$   
there 3 bits and parity for 3 even and  $P_4 = 1$

$P_4$  &  $P_1$  are not equal to zero so received code is wrong.

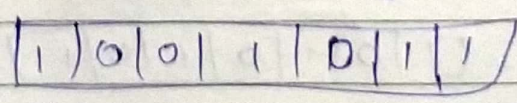
Correcting error:  
error word ⇒ 

$P_4$	$P_2$	$P_1$
1	0	1

  
decimal value = (5)<sub>10</sub>

This show that 5th bit is in error

So we write the correct word by simply inverting the 5th bit



Ex 1110101 Even  
 $D_7 \ D_6 \ D_5 \ P_4 \ D_3 \ P_2 \ P_1$   

1	1	1	0	1	0	1
---	---	---	---	---	---	---

Step 1 check bit 4, 5, 6, 7  
 $P_4 \ D_5 \ D_6 \ D_7 \rightarrow 0 \ 1 \ 1 \ 1 \rightarrow$  odd parity  
 There error exists  $P_4 = 1$

Step 2 check bit 2, 3, 6, 7  
 $P_2 \ D_3 \ D_6 \ D_7 \rightarrow 0 \ 1 \ 1 \ 1 \rightarrow$  odd parity  
 There error exists  $P_2 = 1$

Step 3 check bit 1, 3, 5, 7  
 $P_1 \ D_3 \ D_5 \ D_7 \rightarrow 1 \ 1 \ 1 \ 1 \rightarrow$  even parity  
 There is no error  $P_1 = 0$

Error word  $E = [P_4 \ P_2 \ P_1] \rightarrow [1 \ 1 \ 0]$

$E = (6)_{10}$

Hence bit 6 of the transmitted word is in error

1	1	1	0	1	0	1
---	---	---	---	---	---	---

↑  
 Incorrect bit

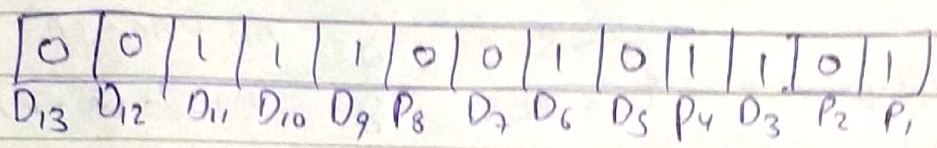
Correct Code — Invert the incorrect bit

1	0	1	0	1	0	1
---	---	---	---	---	---	---

Q

0 0 1 1 1 0 0 1 0 1 1 0 1 odd

Sol



Check

check bit 8, 9, 10, 11, 12, 13

$P_8 D_9 D_{10} D_{11} D_{12} D_{13} \rightarrow 0 1 1 1 0 0$  odd parity  
There is not error  $P_8 = 0$

check

check bit 4, 5, 6, 7, 12, 13, ~~14, 15~~

$P_4 D_5 D_6 D_7 D_{12} D_{13} \rightarrow 1 0 1 0 0 0$  even parity  
There is error  $P_4 = 1$

check

check bit 2, 3, 6, 7, 10, 11, ~~14, 15~~

$P_2 D_3 D_6 D_7 D_{10} D_{11} \rightarrow 0 1 1 0 1 1$  even parity  
There is error  $P_2 = 1$

check

bit 1, 3, 5, 7, 9, 11, 13, ~~15~~

$P_1 D_3 D_5 D_7 D_9 D_{11} D_{13} \rightarrow 1 1 0 0 1 1 0$  odd parity

Error expect  $P_1 = 1$

Error word  $E =$ 

$P_8$	$P_4$	$P_2$	$P_1$
0	1	1	1

$E = (7)_{10}$

In transmitted word 7<sup>th</sup> bit is in error  
Inverted 7<sup>th</sup> bit

0 0 1 1 0 0 1 1 0 1 1 0 1